Assignment: 5
Due: Tuesday, October 25, 2022 9:00 pm
Coverage: End of Module 08 (see Coverage note below)
Language level: Beginning Student with List Abbreviations
Files to submit: cs135search.rkt, tictactoe.rkt

• Make sure you read the OFFICIAL A05 post on Piazza for the answers to frequently asked questions.

• Unless otherwise specified, you may only use Racket language features we have covered up to the coverage point above (End of Module 08).

• It is likely that your functions will not be very efficient, and may be slow on long lists. There is no need to test your functions with excessively long lists.

• The names of functions we tell you to write, and symbols and strings we specify must match the descriptions in the assignment questions exactly. Any discrepancies in your solutions may lead to a severe loss of correctness marks. Basic test results will catch many, but not necessarily all of these types of errors.

• Policies from Assignment A04 carry forward, including:
  – For each function you are required to write, you are also required to submit the design recipe.
  – You are required to submit examples by Friday, October 21 at 8:00AM (before the due date of assignment A05). See the Example Submissions and Basic Test Results post on Piazza for examples of correct and incorrect example submissions.
  – More details about the design recipe grading are specified in the A02 Official Post on Piazza.
Here are the assignment questions you need to solve and submit.

1. **Complete all the required stepping problems in Module 08: Nested Lists** at

   [https://www.student.cs.uwaterloo.ca/~cs135/assign/stepping/](https://www.student.cs.uwaterloo.ca/~cs135/assign/stepping/)

   You should refer to the instructions from **A01 Question 1** for the stepper question instructions.

2. When using Google to find documents on the web, there are a variety of options available. For example, if you searched for two search terms, say *Association* and *List*, you would get web pages that contain both the words *Association* and *List*. If you searched for *Association* and -*List* you would get web pages that contain *Association* but do not contain *List*.

   When looking for all the occurrences of a word in a collection of documents (such as web pages) rather than searching all the documents sequentially, a more efficient approach would be to use an inverted list (also called an inverted index). For this question, we will represent an inverted list as an association list where the key is the search term and the value is a list of all the documents that the search term occurs in. The list of documents that contain the key is called a **doc-list (DL)**.

   ```racket
   ;; A doc-list (DL) is one of:
   ;; * empty
   ;; * (cons Str DL)
   ;; Requires: each doc (i.e. Str) only occurs once in the doc-list
   ;;           the doc-list is in lexicographic order
   ```

   Lexicographic order is the order determined by the Racket function `string<?`, i.e. if `(string<? "a.txt" "b.txt")` is true then "a.txt" should appear in the **doc-list** before "b.txt".

   An **Inverted List** is defined as follows.

   ```racket
   ;; An Inverted List (IL) is one of:
   ;; * empty
   ;; * (cons (list Str DL) IL)
   ;; Requires: each key (i.e. Str) only occurs once in the IL.
   ;;           the keys occur in lexicographic order in the IL.
   ```

   For example, the following three documents were used to build an **Inverted List**.

<table>
<thead>
<tr>
<th>Document Name</th>
<th>Contents</th>
</tr>
</thead>
<tbody>
<tr>
<td>1 a.txt</td>
<td>the cat sleeps</td>
</tr>
<tr>
<td>2 b.txt</td>
<td>the dog barks</td>
</tr>
<tr>
<td>3 c.txt</td>
<td>suddenly the dog chases the cat</td>
</tr>
</tbody>
</table>

   The **Inverted List** would look like the following.
(list (list "barks"  (list "b.txt")))
(lis"cat"  (list "a.txt" "c.txt"))
(list "chases" (list "c.txt"))
(list "dog"  (list "b.txt" "c.txt"))
(list "sleeps" (list "a.txt"))
(list "suddenly" (list "c.txt"))
(list "the"  (list "a.txt" "b.txt" "c.txt")))

E.g. "barks" only appears in the document "b.txt" so the doc-list (DL) for "barks" is
(list "b.txt")

You may use the following string comparison predicates string<?, string<=?, string=?,
string>? and string>=? for this question. You may not use member?.

Hint: You can take advantage of the fact that the lists are sorted in ascending order to make
the search easier. Also be aware that the doc-lists can be different lengths.

(a) Create a function both which consumes two DLs and produces a doc-list (DL) that occur
in both DLs. For example,
(both (list "b.txt") (list "b.txt" "c.txt")) should produce (list "b.txt").

(b) Create a function exclude which consumes two DLs and produces a doc-list (DL) that
occur in the first DL but not the second one. For example,
(exclude (list "b.txt" "c.txt") (list "b.txt")) should produce (list "c.txt").

(c) Create a function (keys-retrieve doc an-il) which consumes a Str and an IL and
produces a (listof Str) with lexicographic ordering. The values in the produced list
are the keys from an-il whose doc-lists contain doc. If doc is not contained in the
doc-list associated with any keys in an-il, then keys-retrieve returns empty.

For example, if we passed "a.txt" and the IL shown at the top of this page to keys-retrieve,
it would return (list "cat" "sleeps" "the").

(d) Create a function search which consumes a Sym, two Strs and an IL. It produces a
doc-list (DL). The arguments for search will always be in one of two possible formats:

- (search 'both str1 str2 an-il) which, given two keys str1 and str2 from
  an-il, produces a doc-list (DL) containing the documents that are present in both
  of the keys’ associated doc-lists.
  For example, if we pass 'both, "barks", "dog" and the IL at the top of the page
  into search, then it would return (list "b.txt").
- (search 'exclude str1 str2 an-il) which, given two keys str1 and str2
  from an-il, produces a doc-list (DL) containing the documents that are present in
  the doc-list associated with the key str1, but not the key str2.

Place your solutions in the file cs135search.rkt
3. In this question you will be playing a large game of Tic-Tac-Toe. In this game players take turn placing Xs and Os in a 3x3 grid, with the X player making the first move. A player wins if they managed to fill a row, column, or diagonal with their letter. If there are no free spots, the game is a draw.

In this question you will deal with an $N \times N$ grid, where $N$ is an odd natural number.

We can represent such a grid in Racket using lists of lists.

```racket
;; A Tic-Tac-Toe Grid (T3Grid) is a (listof (listof (anyof 'X 'O '_)))
;; Requires: all lists have the same length, and that length is odd
;; The number of 'X and 'O is equal, or there is one more 'X

Here, the symbols 'X and 'O (A capital “Oh”, not a zero) represent the X and O player, and the symbol '_' represents a blank square.

Examples
Standard 3x3 Grid, no moves
(define grid1
  (list (list '_ '_ '_)
        (list '_ '_ '_)
        (list '_ '_ '_)))

5x5 grid, 4 X moves, 4 O moves
(define grid2
  (list (list 'X 'O 'O 'O '_)
        (list 'X 'X 'O '_ '_)
        (list '_ '_ '_ '_ '_)
        (list '_ '_ '_ '_ 'X)))

Tiny 1x1 grid, 1 X move, no O moves.
(define grid3
  (list (list 'X)))
```
Because players take turns, the number of Xs will either be equal to the number of Os, or else it will be one greater than the number of Os. As always, you do not need to check this requirement (it is part of the data definition, so it can safely be assumed).

Additionally, for any functions that consume a row number and/or a column number, these numbers are required to be valid. They start counting from 0, so, $0 \leq$ row number, column number $< N$ (where $N$ is the number of rows and columns in the grid).

For this question (and only this question) you may use the \texttt{list-ref} function.

(a) Write the function \texttt{whose-turn} that consumes a \texttt{T3Grid} and determines whose turn it is. X goes first, so if the number of Xs and Os is equal, X goes next (produce \texttt{'X}). If the number of Xs is 1 greater than the number of Os, O goes next (produce \texttt{'O}).

Examples: In \texttt{grid1} and \texttt{grid2} X goes next. In \texttt{grid3} O goes next (the game is over since the grid is full, but the function is still defined since that is a valid \texttt{T3Grid}).

(b) Write the function \texttt{grid-ref} that consumes a \texttt{T3Grid} and a row and column number, and produces the symbol located at that location. Row and column numbers start counting from 0.

Examples:

\begin{verbatim}
(check-expect (grid-ref grid2 1 2) 'O)
(check-expect (grid-ref grid2 0 0) 'X)
\end{verbatim}

(c) Part of figuring out if a player has won is seeing if they have filled in a row or a column. Finding a row is easy, since each row already in list form. Columns, on the other hand, are spread across multiple lists. So, it would be nice to be able to convert them into a list.

Write the function \texttt{get-column} that consumes a \texttt{T3Grid}, and a column number, and produces a list of the symbols in that column.

Examples:

\begin{verbatim}
(check-expect (get-column grid1 0) (list '_ '_ '_))
(check-expect (get-column grid2 1) (list 'O 'X '_ '_ '_))
(check-expect (get-column grid3 0) (list 'X))
\end{verbatim}

(d) Write the function \texttt{will-win?} that consumes a \texttt{T3Grid}, a row number, a column number, and a player (either \texttt{'X} or \texttt{'O}). The function produces true if that player would win by placing a marker at the given location, and false otherwise. Note that if the given location is not blank, then the player will not win (you cannot win by making an illegal move).

To keep things simple, you do not need to worry about checking the diagonals, only rows and columns.

You may assume that nobody has won yet in the consumed board.
Examples:

(check-expect (will-win? grid1 0 0 'X) false)
(check-expect (will-win? (list (list 'X 'X '_)
                    (list 'O 'X 'O)
                    (list 'O '_ '_))
                    0 2 'X) true)

Place your solutions in tictactoe.rkt

This concludes the list of questions for which you need to submit solutions. Don’t forget to always check your email for the basic test results after making a submission.