

Pseudocode

In lectures, algorithms will often be expressed in pseudocode, a mixture of code and English. While understanding pseudocode is usually not difficult, writing it can be a challenge.

One example of pseudocode, used in this course, is presented in Section 2. Section 3 contains examples of pseudocode found in various textbooks.

1 Guidelines for writing pseudocode

Why use pseudocode at all? Pseudocode strikes a sometimes precarious balance between the understandability and informality of English and the precision of code. If we write an algorithm in English, the description may be at so high a level that it is difficult to analyze the algorithm and to transform it into code. If instead we write the algorithm in code, we have invested a lot of time in determining the details of an algorithm we may not choose to code (as we typically wish to analyze algorithms *before* deciding which one to code). The goal in writing pseudocode, then, is to provide a high-level description of an algorithm which facilitates analysis and eventual coding (should it be deemed to be a “good” algorithm) but at the same time suppresses many of the details that vanish with asymptotic notation. Finding the right level in the tradeoff between readability and precision can be tricky. If you have questions about the pseudocode you are writing on an assignment, please ask one of the course personnel to look it over and give you feedback (preferably before you hand it in so you can change it if necessary).

Just as a proof is written with a type of reader in mind (hence proofs in undergraduate textbooks tend to have more details than those in journal papers), algorithms written for different audiences may be written at different levels of detail. In assignments and exams for the course, you need to demonstrate your knowledge without obscuring the big picture with unneeded detail. Here are a few general guidelines for checking your pseudocode:

1. Mimic good code and good English. Using aspects of both systems means adhering to the style rules of both to some degree. It is still important that variable names be mnemonic, comments be included where useful, and English phrases be comprehensible (full sentences are usually not necessary).
2. Ignore unnecessary details. If you are worrying about the placement of colons, you are using too much detail. It is a good idea to use some convention to group statements (begin/end, brackets, or whatever else is clear), but you shouldn't obsess about syntax.
3. Don't belabour the obvious. In many cases, the type of a variable is clear from context; unless it is critical that it is specified to be an integer, for example, it is often unnecessary to make it explicit.
4. Take advantage of programming shorthands. Using branching or looping structures is more concise than writing out the equivalent in English; general constructs that are not

peculiar to a small number of languages are good candidates for use in pseudocode. Using parameters when defining functions is concise, clear, and accurate, and hence should be included in your pseudocode.

5. Consider the context. If you are writing an algorithm for mergesort, the statement “Use mergesort to sort the values” is hiding too much detail; if we have already studied mergesort in class and later use it as a subroutine in another algorithm, the statement would be appropriate to use.
6. Don’t lose sight of the underlying model. It should be possible to “see through” your pseudocode to the model below; if not (that is, you are not able to analyze the algorithm easily), it is written at too high a level.
7. Check for balance. If the pseudocode is hard for a person to read or difficult to translate into working code (or worse yet, both!), then something is wrong with the level of detail you have chosen to use.

2 Pseudocode used in the course

The pseudocode used in the course will adhere to the following conventions:

- Variable names are capitalized, and function names are written in all capital letters. Where helpful for readability, such as to separate words, an underscore (`_`) is used.
- To make it distinguishable from code, which is presented in **typewriter font**, pseudocode is presented using *italics*. (The one exception is function names, which may be written with or without italics.)
- Simple Python list operations, such as `[]` for an empty list or accessing an item in a position, will be included, but no powerful operations, such as `sorted` and `reverse`.
- The Python list operation slice can be used, with the indices having the same meaning as in Python: `[a:b]` consists of items *a* up to but not including *b*, where if *a* is omitted the slice starts at the first item in the list and if *b* is omitted the last item in the slice is the last item in the list. The operation can also be used for strings.
- The Python method `len` will be written as `LENGTH` for consistency with other names.
- Each function definition contains a preamble consisting of the name of the function and parameters, the input, the output (if any), and side effects (if any).
- Function applications are given as the name of the function with all parameters appearing afterwards in parentheses, separated by commas. For consistency, instead of using dot notation for methods, the object appears as one of the inputs. For example, to determine the length of list *L* we would write `LENGTH(L)`.
- Reserved words (such as ***for*** and ***if***) are shown in boldface.

- Assignment statements are shown using \leftarrow , like in Example 3. Other common conventions are the use of $=$ (Example 4) and $:=$ (Example 2).
- Types of variables are not listed explicitly, unlike in Examples 2 (which uses `integer`) and 4 (which uses `int`). Ideally, the code will be written in such a way that the type is clear from context, or from the listing of inputs and outputs.
- Indentation is used to group statements, like in Python.
- The word *return* is used to indicate that a value is returned.
- Branching mimics Python; thus, *if* and *else* are used, but unlike in Examples 1–3, not *then*.
- In *for* loops, a loop that goes from the value *Start* to the value *Finish* will be written *for Count from Start to Finish*, where *Count* can be replaced by a variable of another name. The comparable Python code would be `for count in range(start, finish+1)`.
- For a *for* loop over a list or other collection, *for each ... in* is used, such as *for each Item in List*.
- For the ease of analysis, almost always a line will contain a finite number of simple tasks (cost $\Theta(1)$) or a function application.

As you can see from the example of binary search below, the pseudocode is quite close to Python.

```

BIN_SEARCH(L, Item)
INPUT:      A list L with items in nondecreasing order
OUTPUT:    True or False depending on whether Item is in L
if LENGTH(L)  $\leq$  1
    if LENGTH(L) == 1 and L[0] == Item
        return True
    else
        return False
else
    Mid = FLOOR(LENGTH(L) / 2)
    if L[Mid] == Item
        return True
    else if L[Mid] > Item
        return BIN_SEARCH(L[:Mid], Item)
    else
        return BIN_SEARCH(L[Mid+1:], Item)

```

3 Pseudocode style examples

Various styles of pseudocodes can be observed in these examples of the binary search algorithm. Not all of these examples are worth emulating, as some are too detailed and some are hard to understand.

Example 1 The Design and Analysis of Computer Algorithms, Aho, Hopcroft, and Ullman, 1974, page 114.

```

procedure SEARCH(a, f, ℓ):
if f > ℓ then return "no"
else
  if a = A[⌊(f+ℓ)/2⌋] then return "yes"
  else
    if a < A[⌊(f+ℓ)/2⌋] then
      return SEARCH(a, f, ⌊(f+ℓ)/2⌋ - 1)
    else return SEARCH(a, ⌊(f+ℓ)/2⌋ + 1, ℓ)

```

Example 2 Algorithms, Robert Sedgewick, 1988, p. 198.

```

function binarysearch(v:integer):integer;
  var x, ℓ, r:integer;
  begin
    ℓ:=1; r:=N;
  repeat
    x:=(ℓ+r)div 2;
    if v<a[x].key then r:=x-1 else ℓ:=x+1
  until (v=a[x].key) or (ℓ > r);
  if v=a[x].key
    then binarysearch:=x
    else binarysearch:=N + 1
  end;

```

Example 3 Data Structures and Their Algorithms, Lewis and Denenberg, 1991, p. 182.

```

function BinarySearchLoopUp(key K, table T[0..n-1]): info
{Return information stored with key K in T, or Λ if K is not T}
  Left ← 0
  Right ← n-1
  repeat forever
    if Right < Left then
      return Λ
    else
      Middle ← ⌊ (Left + Right)/2 ⌋
      if K = Key(T[Middle]) then return info(T[Middle])

```

```
else if  $K < \text{Key}(T[\text{Middle}])$  then  $\text{Right} \leftarrow \text{Middle} - 1$   
else  $\text{Left} \leftarrow \text{Middle} + 1$ 
```

Example 4 Computer Algorithms: Introduction to Design and Analysis, Baase and Van Gelder, 2000, p. 129

```
int binarySearch(int[], E, int first, int last, int K)  
  if (last < first)  
    index = -1;  
  else  
    int mid = (first + last)/2;  
    if (K == E[mid])  
      index = mid;  
    else if (K < E[mid])  
      index = binarySearch(E, first, mid-1, K);  
    else  
      index = binarySearch(E, mid+1, last, K);  
  return index;
```