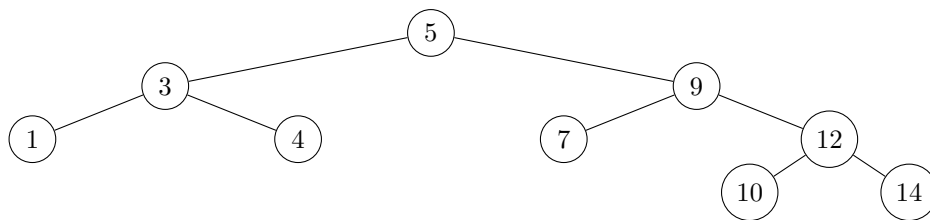


Tutorial 05: Feb 12

1. **Double Right Rotation is Not Two Right Rotations**

Consider following AVL tree. Perform `delete(5)`, using only

- Right rotation or Left rotation
- Double right rotation or Double left rotation
- Starting from an empty binary search tree, in what order should we add the integers 1, 3, 4, ..., 14 to obtain the tree below?



If you have a choice of which element to move up, pick the inorder successor, which is 7.

2. **Partial Sum**

Consider the problem where we have a sequence of n elements: $S = a_1, a_2, \dots, a_n$, and 3 operations:

- $Add(S, b) \rightarrow a_1, a_2, \dots, a_n, b$
- $Update(S, i, \Delta) \rightarrow a_1, \dots, a_{i-1}, \Delta, a_{i+1}, \dots, a_n$
- $PartialSum(S, k) \rightarrow \sum_{i=1}^k a_i$

Design a data structure that can perform each of these operations in $O(\log n)$ expected time.

3. **Height of AVL Tree**

Describe an algorithm for computing the height of AVL tree in $O(\log n)$ time, where n is the number of elements in given AVL tree. In addition, you may assume that balance factor for each node is pre-computed correctly. Moreover, assume that you are given a pointer/node of the root of AVL tree.