Midterm Review

CS348 Spring 2025: Introduction to Database Management

> Instructor: Xiao Hu Sections: 001, 002, 003

Announcements

- Appealing of Assignment 1
 - Check remark request guidelines on Piazza
 - Reach out to corresponding TA, IA (Guy), ISC (Sylvie)
 - Check sample solutions on Learn
- Milestone 1 of Group Project
 - Due on June 19
- Switch-type cut-off for assessment
 - Due on June 19
- Assignment 2
 - Coverage: Lecture 4 Lecture 12
 - Check online office hours on Piazza
 - Due on June 24

Midterm Exam

- Logistics
 - Time & Date: 4:30 PM 6:00 PM June 27
 - Location: M3 1006 and STC 0040 (check your room)
 - All contents in Lectures 1 12 (no optional parts)
 - Closed book, but a two-page reference sheet will be provided (already released on Learn)
- How to prepare (in addition to lectures)?
 - Sample questions released on Learn
 - Partial solutions to be released later on Learn
 - A1 (with partial solutions) and A2

Relational Model and Relational Algebra

Relational data model

- A database is a collection of relations (or tables)
- Each relation has a set of attributes (or columns)
- Each attribute has a unique name and a domain (or type)
 - The domains are required to be **atomic**

Single, indivisible piece of information

- Each relation contains a set of tuples (or rows)
 - Each tuple has a value for each attribute of the relation
 - Duplicate tuples are not allowed

Types of integrity constraints

- Tuple-level
 - Domain restrictions, attribute comparisons, etc.
 - E.g. *age* cannot be **negative**
 - E.g. for flights table, arrival time > take off time
- Relation-level
 - Key constraints
 - E.g. uid should be unique in the User relation
 - Functional dependencies (Lecture 11)
- Database-level
 - Referential integrity foreign key
 - *uid* in *Member* must refer to a row in *User* with the same *uid*

Key (Candidate Key)

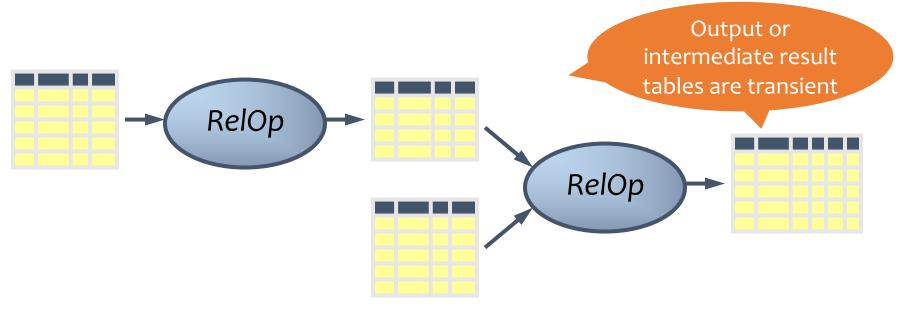
A set of attributes *K* for a relation *R* is a key if

- Condition 1: In no instance of *R* will two different tuples agree on all attributes of *K*
 - That is, *K* can serve as a "tuple identifier"
- Condition 2: No proper subset of *K* satisfies the above condition
 - That is, *K* is minimal
- Example: User (uid, name, age, pop)
 - uid is a key of User
 - age is not a key (not an identifier)
 - {uid, name} is not a key (not minimal), but a superkey
- One candidate key is assigned to be primary key

Satisfies only Condition 1

Relational algebra

- A language for querying relational data based on "operators"
- Set semantics



Summary of operators

Core Operators

- 1. Selection: $\sigma_p R$
- 2. Projection: $\pi_L R$
- 3. Cross product: $R \times S$
- 4. Union: *R* ∪ *S*
- 5. Difference: R S
- 6. Renaming: $\rho_{S(A_1 \rightarrow A'_1, A_2 \rightarrow A'_2, \dots)} R$

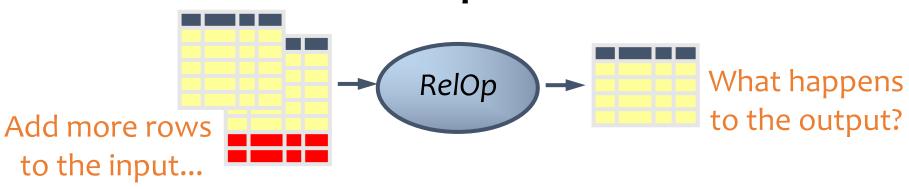
Derived Operators

- 1. Join: $R \bowtie_p S$
- 2. Natural join: $R \bowtie S$
- 3. Intersection: $R \cap S$
- 4. Division: $R \div S$

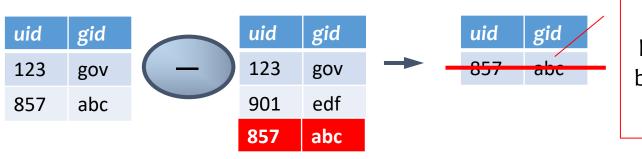
Note: Only use these operators for assignments & exams

Note: Outerjoin is also allowed.

Non-monotone operators



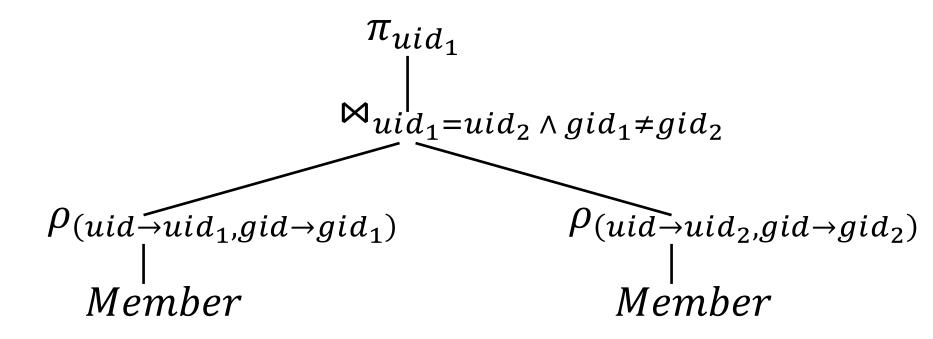
- If some old output rows may become invalid, and need to be removed → the operator is non-monotone
- Otherwise (old output rows always remain "correct") → the operator is monotone



This old row becomes invalid because the new row added to S

Expression tree notation

IDs of users who belong to at least two groups

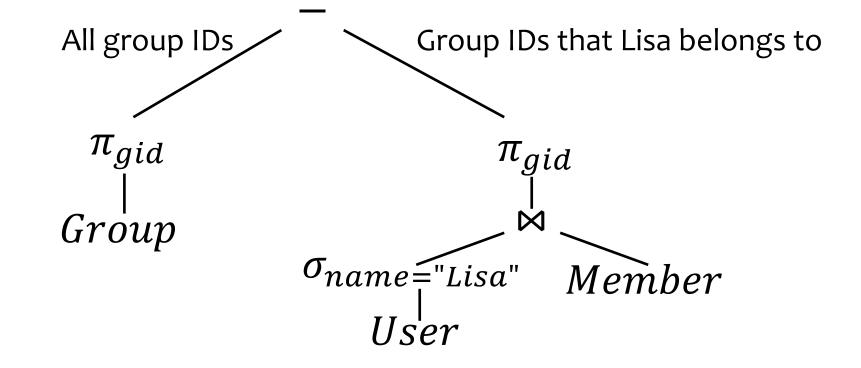


IDs of groups that contain at least two users

An example

User (<u>uid</u> int, name string, age int, pop float) Group (<u>gid</u> string, name string) Member (<u>uid</u> int, <u>gid</u> string)

• IDs of groups that Lisa doesn't belong to

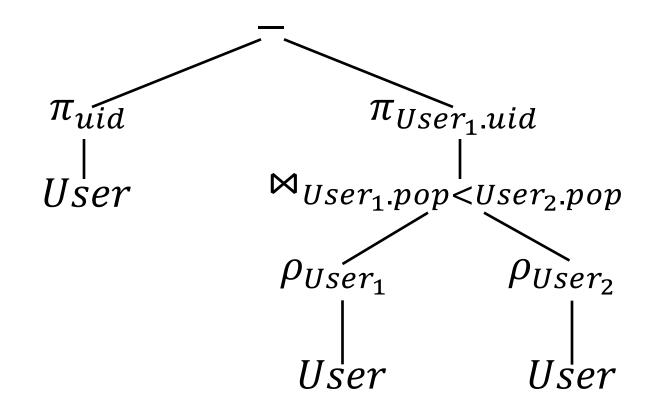


 $(\pi_{gid}Group) - (\pi_{gid}((\sigma_{name="Lisa"}User) \bowtie Member))$

Most popular user

User (<u>uid</u> int, name string, age int, pop float) Group (<u>gid</u> string, name string) Member (<u>uid</u> int, <u>gid</u> string)

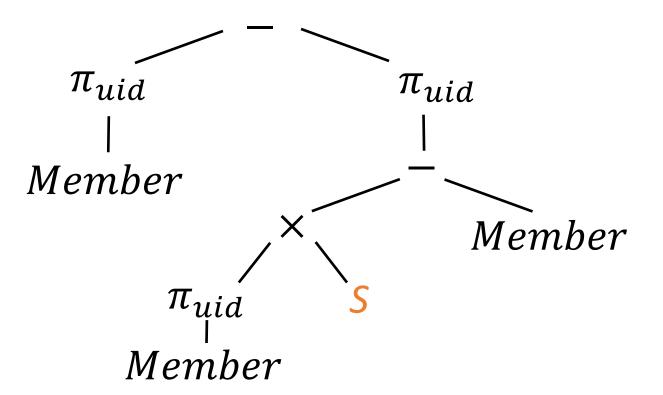
- Who are the most popular?
 - Who do NOT have the highest pop rating?
 - Whose pop is lower than somebody else's?



Division

User (<u>uid</u> int, name string, age int, pop float) Group (<u>gid</u> string, name string) Member (<u>uid</u> int, <u>gid</u> string)

- Who joins all the groups that Lisa joins?
 - All groups (ids) that Lisa belongs to Suppose as S(gid)
 - Who joins all groups in S?
 - Who does not join some group in S?



SQL

Summary of SQL

- Basic topics
 - Data-definition language (DDL): define/modify schemas, drop relations
 - Data-manipulation language (DML): query data
 - SELECT-FROM-WHERE
 - DISTINCT, UNION/EXCEPT/INTERSECT (ALL)
 - Table, Scalar, IN, EXISTS, ALL, ANY)
 - GROUP BY, HAVING
 - ORDER
 - NULL and JOIN and modify data (INSERT/DELETE/UPDATE)
 - Constraints (NOT NULL, UNIQUE, PRIMARY/FOREIGN KEY, CHECK, ASSERTION)
- Advanced topics
 - View, Triggers, Recursion, Index, Programming (optional)

DDL

User (<u>uid</u> int, name string, age int, pop float)⁷ Group (<u>gid</u> string, name string) Member (<u>uid</u> int, <u>gid</u> string)

• **CREATE TABLE** table_name (..., name type, ...);

CREATE TABLE User(uid INT, name VARCHAR(30), age INT, pop DECIMAL(3,2)); CREATE TABLE Group (gid CHAR(10), name VARCHAR(100)); CREATE TABLE Member (uid INT, gid CHAR(10));

DROP TABLE table_name;

DROP TABLE User; DROP TABLE Group; DROP TABLE Member;

ALTER TABLE table_name;

Drastic action: deletes ALL info about the table, not just the contents

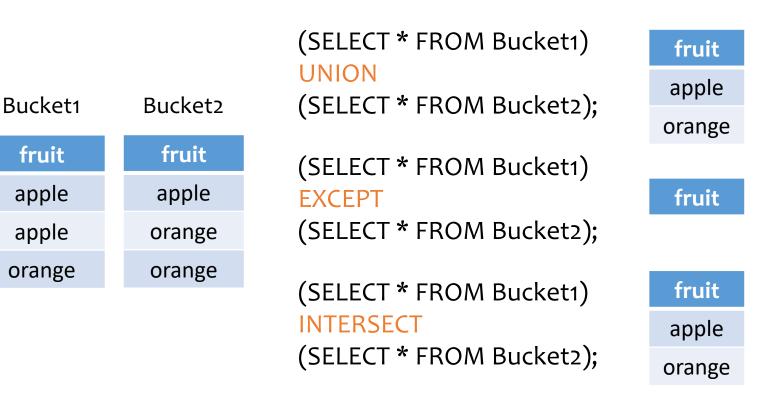
ALTER TABLE Member ADD date; ALTER TABLE Member RENAME date TO mdate; ALTER TABLE Member DROP mdate;

Basic queries for DML: SFW statement

- SELECT (DISTINCT) $A_1, A_2, ..., A_n$ FROM $R_1, R_2, ..., R_m$ WHERE condition;
- Also called an SPJ (select-project-join) query
- Corresponds to (but not really equivalent to) relational algebra query: $\pi_{A_1,A_2,...,A_n}(\sigma_{condition}(R_1 \times R_2 \times \cdots \times R_m))$

SQL set operations

- Set: UNION, EXCEPT, INTERSECT
 - Exactly like set U, —, and ∩ in relational algebra
 - Duplicates in input tables, if any, are first eliminated
 - Duplicates in result are also eliminated



SQL bag operations

- Bag: UNION ALL, EXCEPT ALL, INTERSECT ALL
 - Think of each row as having an implicit count (the number of times it appears in the table)

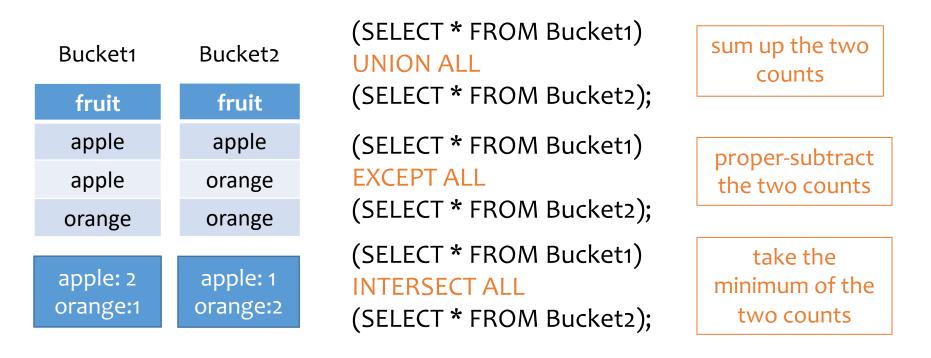


Table subqueries

- Query result as a table that can be used in FROM, set/bag operations, etc.
 - Temporarily exist only in the duration of the outer query
- Example: names of users belonging to at least two groups

```
SELECT name
FROM User,
(SELECT DISTINCT m1.uid
FROM Member m1, Member m2
WHERE m1.uid=m2.uid AND m1.gid != m2.gid) AS temp
WHERE User.uid = temp.uid;
```

WITH clause

User (<u>uid</u> int, name string, age int, pop float) Group (<u>gid</u> string, name string) Member (<u>uid</u> int, <u>gid</u> string)

- Another way of defining a temporary table
 - Available only to the query in which the WITH clause occurs
- Example: names of users belonging to at least two groups

WITH temp AS (SELECT DISTINCT m1.uid FROM Member m1, Member m2 WHERE m1.uid=m2.uid AND m1.gid != m2.gid) SELECT name FROM User, temp WHERE User.uid = temp.uid;

Scalar subqueries

User (<u>uid</u> int, name string, age int, pop float) Group (<u>gid</u> string, name string) Member (<u>uid</u> int, <u>gid</u> string)

- A query that returns a single row can be used as a value in SELECT, WHERE, etc.
- Example: users at the same age as Bart

```
SELECT *
FROM User
WHERE age = (SELECT age
FROM User
WHERE name = 'Bart');
```

- When can this query go wrong?
 - Return more than 1 row
 - Return no rows or NULL values

IN subqueries

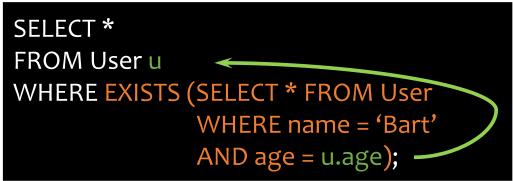
- x IN (subquery) checks if x is in the result of subquery
- Example: users at the same age as (some) Bart

SELECT * FROM User, WHERE age IN (SELECT age FROM User WHERE name = 'Bart');

EXISTS subqueries

User (<u>uid</u> int, name string, age int, pop float) Group (<u>gid</u> string, name string) Member (<u>uid</u> int, <u>gid</u> string)

- EXISTS (*subquery*) checks if the result of *subquery* is non-empty
 - True if at least one row is returned by subquery
- Example: users that have the same age as (some) Bart



• This happens to be a correlated subquery -- a subquery that references tuple variables in surrounding queries

Quantified subqueries

- Universal quantification (for all):
 - ... WHERE *x* op ALL(subquery) ...
 - True if for all *t* in the *subquery* result such that *x op t* is true

SELECT * FROM User WHERE pop >= ALL (SELECT pop FROM User);

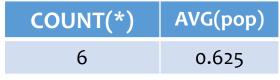
- Existential quantification (exists):
 - ... WHERE *x* op ANY(subquery) ...
 - True if there exists some *t* in the *subquery* result such that *x* op *t* is true

SELECT * FROM User WHERE NOT (pop < ANY (SELECT pop FROM User));

Aggregates

- Standard SQL aggregate functions: COUNT, SUM, AVG, MIN, MAX
- Example: number of users under 18, and their average popularity

SELECT COUNT(*), AVG(pop) FROM User WHERE age <18;



- Aggregate functions do not appear in WHERE clause
- Aggregate with DISTINCT

SELECT COUNT(DISTINCT uid) FROM Member;

GROUP BY

SELECT age, AVG(pop) FROM User GROUP BY age;

uid	name	age	рор
142	Bart	10	0.9
857	Lisa	8	0.7
123	Milhouse	10	0.2
456	Ralph	8	0.3

Compute GROUP BY: group rows according to the values of GROUP BY columns

	uid	name	age	рор
	142	Bart	10	0.9
	123	Milhouse	10	0.2
	857	Lisa	8	0.7
1	456	Ralph	8	0.3

Compute SELECT for each group

age

10

8

avg_pop

0.55

0.50

HAVING

- Used to filter groups based on the group properties (e.g., aggregate values, GROUP BY column values)
- List the average popularity for each age group with more than a hundred users

SELECT age, AVG(pop) FROM User GROUP BY age HAVING COUNT(*)>100; SELECT T.age, T.apop FROM (SELECT age, AVG(pop) AS apop, COUNT(*) AS gsize FROM User GROUP BY age) AS T WHERE T.gsize>100;

ORDER BY and LIMIT

• List the top 3 users after sorting them by popularity (descending) and name (ascending)

SELECT uid, name, age, pop FROM User ORDER BY pop DESC, name LIMIT 3;

- ASC is the default option
- The LIMIT clause specifies the number of rows to return

Three-valued logic - NULL

TRUE = 1, FALSE = 0, UNKNOWN = 0.5 $x \text{ AND } y = \min(x, y)$ $x \text{ OR } y = \max(x, y)$ NOT x = 1 - x

X	у	x AND y	x OR y	NOT <i>x</i>
TRUE	TRUE	TRUE	TRUE	FALSE
TRUE	UNKNOWN	UNKNOWN	TRUE	FALSE
TRUE	FALSE	FALSE	TRUE	FALSE
UNKNOWN	TRUE	UNKNOWN	TRUE	UNKNOWN
UNKNOWN	UNKNOWN	UNKNOWN	UNKNOWN	UNKNOWN
UNKNOWN	FALSE	FALSE	UNKNOWN	UNKNOWN
FALSE	TRUE	FALSE	TRUE	TRUE
FALSE	UNKNOWN	FALSE	UNKNOWN	TRUE
FALSE	FALSE	FALSE	FALSE	TRUE

Rules of Dealing with NULL

- Comparing a NULL with another value (including another NULL) using =, >, etc., the result is NULL
- WHERE and HAVING clauses only select rows for output if the condition evaluates to TRUE
 - FALSE and UNKNOWN are not sufficient
- Aggregate functions ignore NULL, except COUNT(*)
 - SUM, AVG, MIN, MAX all ignore NULLs
 - COUNT(age) also ignores NULL
 - If all inputs are NULL, SUM, AVG, MIN, MAX all return NULL

Unfortunate consequences

• Q1a = Q1b?

Q1a. SELECT AVG(pop) FROM User;

Q1b. SELECT SUM(pop)/COUNT(*) FROM User;

• Q2a = Q2b?

Q2a. SELECT * FROM User;
Q2b SELECT * FROM User WHERE pop=pop;

- Be careful: NULL breaks many equivalences
- Use IS NULL or NOT NULL for NULL comparisons

Full Outerjoin

Group

gid	gname
abc	Book Club
gov	Student Government
dps	Dead Putting Society
spr	Sports Club

Member		
uid	gid	
142	dps	
123	gov	
857	abc	
857	gov	
789	foo	

Group ⋈ Member

gid	gname	uid
abc	Book Club	857
gov	Student Government	123
gov	Student Government	857
dps	Dead Putting Society	142
foo	NULL	789
spr	Sports Club	NULL

A full outerjoin between R and S:

- All rows in the result of $R \bowtie S$, plus
- "Dangling" *R* rows (those that do not join with any *S* rows) padded with NULL's for *S*'s columns
- "Dangling" S rows (those that do not join with any R rows) padded with NULL's for R's columns

Left/Right Outerjoin

Group ⋈ Member

gid	gname	uid
abc	Book Club	857
gov	Student Government	123
gov	Student Government	857
dps	Dead Putting Society	142
spr	Sports Club	NULL

• A left outerjoin $(R \bowtie S)$ includes rows in $R \bowtie S$ plus dangling R rows padded with NULL's

	gid	gname	uid
Group ⋈ Member	abc	Book Club	857
	gov	Student Government	123
	gov	Student Government	857
Z	dps	Dead Putting Society	142
'	foo	NULL	789

• A right outerjoin $(R \bowtie S)$ includes rows in $R \bowtie S$ plus dangling S rows padded with NULL's

Group

gid	gname
abc	Book Club
gov	Student Government
dps	Dead Putting Society
spr	Sports Club

Member		
uid	gid	
142	dps	
123	gov	
857	abc	
857	gov	
789	foo	

Outerjoin in SQL

SELECT * FROM Group JOIN Member ON Group.gid = Member.gid;

SELECT * FROM Group NATURAL JOIN Member;

SELECT * FROM Group LEFT OUTER JOIN Member ON Group.gid = Member.gid;

SELECT * FROM Group **RIGHT OUTER JOIN** Member **ON** Group.gid = Member.gid;

SELECT * FROM Group FULL OUTER JOIN Member ON Group.gid = Member.gid; $\approx Group \underset{Group.gid=Member.gid}{\bowtie} Member$

 \approx Group \bowtie Member

 $\approx Group \underset{Group.gid=Member.gid}{\rightarrowtail} Member$

 $\approx Group_{Group.gid=Member.gid} Member$

 $\approx Group \underset{Group.gid=Member.gid}{\rightarrowtail} Member$

Modify Data

• Insert one row or the results of a query

INSERT INTO Member VALUES (789, 'dps');

INSERT INTO Member (SELECT uid, 'dps' FROM User WHERE uid NOT IN (SELECT uid FROM Member WHERE gid = 'dps'));

• Delete according to a WHERE condition

DELETE FROM Member WHERE uid=789 AND gid='dps';

DELETE m, u FROM Member m NATURAL JOIN User u WHERE age > 18 AND gid = 'abc';

• Update: User 142 changes name to "Barney"

UPDATE User SET name = 'Barney' WHERE uid = 142;

UPDATE User SET pop = (SELECT AVG(pop) FROM User);

Types of SQL constraints

- NOT NULL
- Key
- Referential integrity
- Tuple- and attribute-based CHECK's
- General assertion

Example of NOT NULL

CREATE TABLE User (uid INT NOT NULL, name VARCHAR(30) NOT NULL, twitterid VARCHAR(15), age INT NOT NULL, pop DECIMAL(3,2));

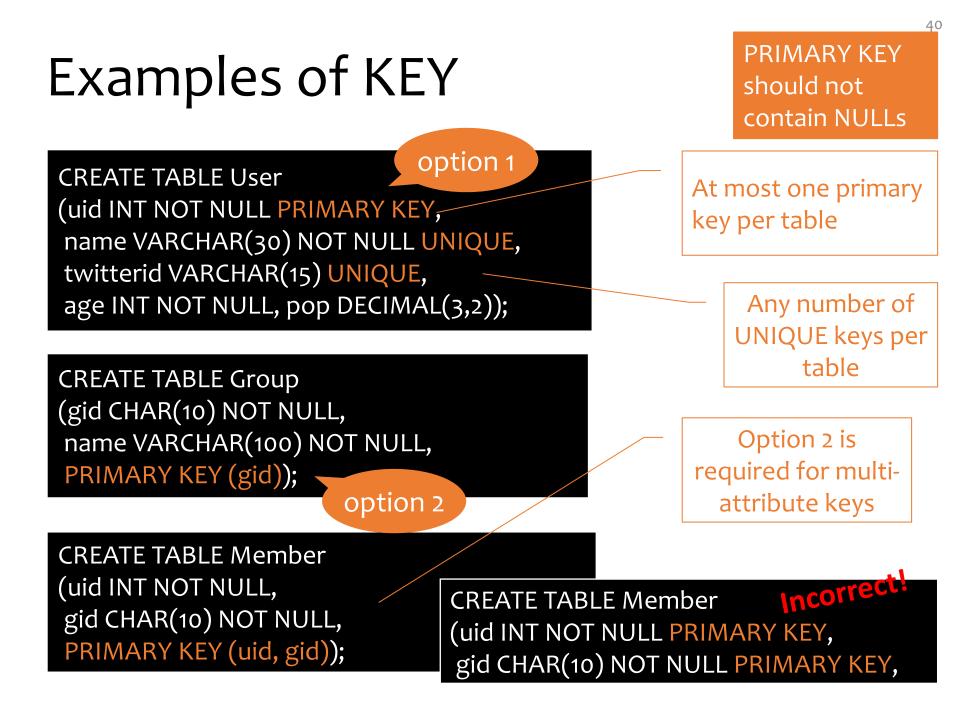
Incorrect

INSERT INTO User (uid, age) VALUES (389, 18);

Incorrect

CREATE TABLE Group (gid CHAR(10) NOT NULL, name VARCHAR(100) NOT NULL); INSERT INTO User VALUES (789, 'Nelson', NULL, NULL, NULL);

CREATE TABLE Member (uid INT NOT NULL, gid CHAR(10) NOT NULL);



Referential integrity in SQL

- Referenced column(s) must be PRIMARY KEY
 - Some systems allow both PRIMARY KEY and UNIQUE
- Referencing column(s) form a FOREIGN KEY
- Example

CREATE TABLE User (... uid INT NOT NULL PRIMARY KEY);

CREATE TABLE Group (... gid CHAR(10) NOT NULL PRIMARY KEY);

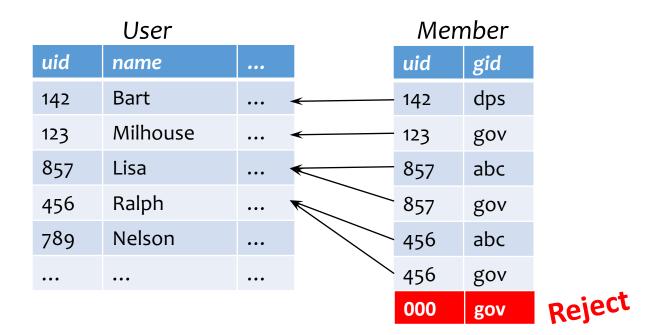
CREATE TABLE Member (uid INT NOT NULL REFERENCES User(uid), gid CHAR(10) NOT NULL, PRIMARY KEY (uid,gid), FOREIGN KEY (gid) REFERENCES Group(gid)); 41

Enforcing referential integrity

Example: Member.uid references User.uid

• Insert or update a Member row whose uid refers to a non-existent uid in User

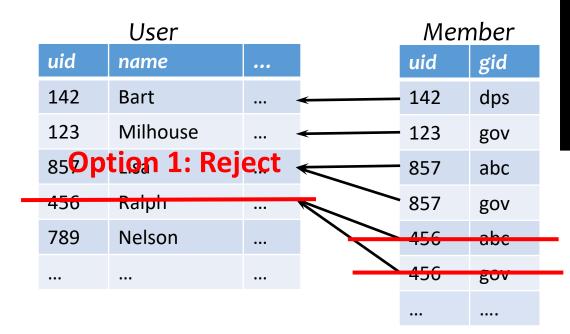
• Reject



Enforcing referential integrity

Example: Member.uid references User.uid

- Delete or update a User row whose uid is referenced by some Member row
 - Multiple Options (SQL)



Option 3: Set NULL

(set all references to NULL)

CREATE TABLE Member (uid INT NOT NULL REFERENCES User(uid) ON DELETE CASCADE,);

Option 2: Cascade (ripple changes to all referring rows)

Tuple- and attribute-based CHECK

- Associated with a single table!
- Only checked when a tuple or an attribute is updated
 - Reject if condition evaluates to FALSE
 - TRUE and UNKNOWN are fine

(Recap) WHERE and HAVING clauses should evaluate to TRUE

• Examples: each user has age above o or NULL

```
CREATE TABLE User(...
age INTEGER CHECK(age IS NULL OR age > 0), ...);
CREATE TABLE User(...
age INT,
CONSTRAINT minAge CHECK(age IS NULL OR age > 0), ...);
```

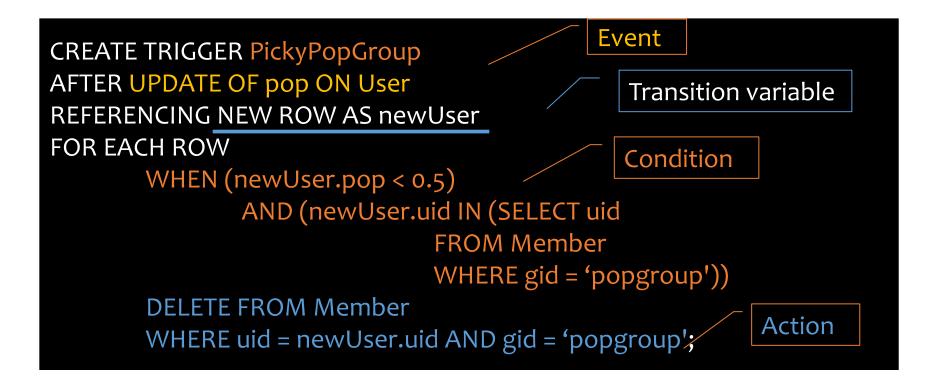
General assertion

- Can involve multiple tables!
- CREATE ASSERTION ... CHECK assertion_condition
- Checked for any modification that could potentially violate it
 - Reject if condition evaluates to FALSE or UNKNOWN
 - TRUE is required
- Example: Member.uid references User.uid

CREATE ASSERTION MemberUserRefIntegrity CHECK (NOT EXISTS (SELECT * FROM Member WHERE uid NOT IN (SELECT uid FROM User))); Checked when Member or User is modified

Triggers

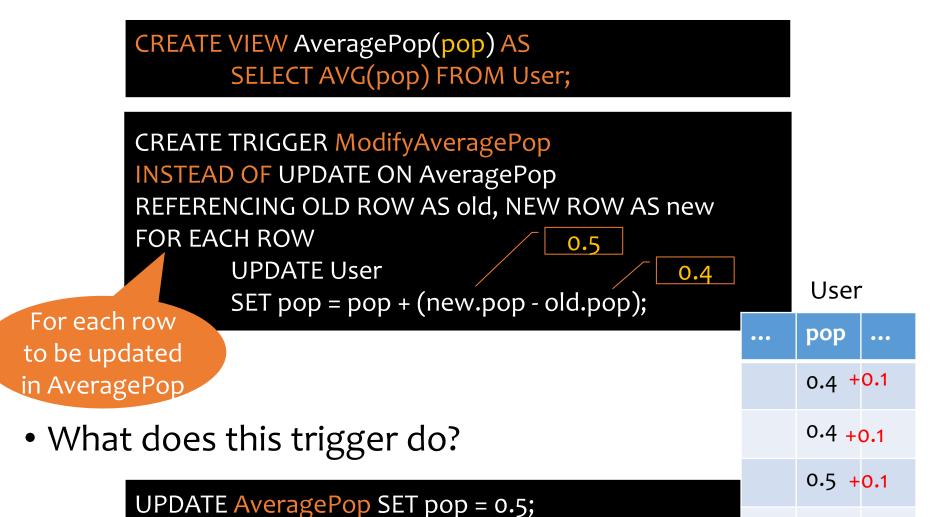
- A trigger is an event-condition-action (ECA) rule
 - When event occurs, test condition; if condition is satisfied, execute action



Trigger options

- Possible events include:
 - INSERT ON table; DELETE ON table; UPDATE [OF column] ON table
- Timing -- action can be executed:
 - AFTER or **BEFORE** the triggering event
 - INSTEAD OF the triggering event on views (lecture 5)
- Granularity -- trigger can be activated:
 - FOR EACH ROW modified
 - NEW ROW and OLD ROW
 - FOR EACH STATEMENT that performs modification
 - NEW TABLE and OLD TABLE
- Certain triggers are only at statement-level

INSTEAD OF triggers for views



0.3 <mark>+0.1</mark>

Views

- A view is like a "virtual" table
 - Defined by a query, which describes how to compute the view contents on the fly
 - Stored as a query by DBMS instead of query contents
 - Can be used in queries just like a regular table

CREATE VIEW PopGroup AS SELECT * FROM User WHERE uid IN (SELECT uid FROM Member WHERE gid = 'popgroup'); SELECT AVG(pop) FROM PopGroup;

DROP VIEW popGroup;

Modifying views

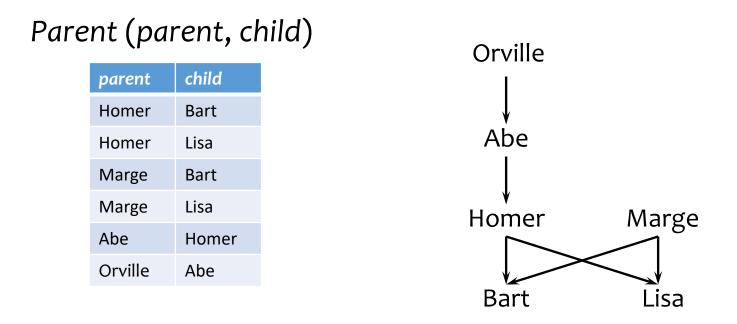
• Goal: modify base tables such that the modification would appear to have been done on the view

CREATE VIEW UserPop AS SELECT uid, pop FROM User; DELETE FROM UserPop WHERE uid = 123;

DELETE FROM User WHERE uid = 123;

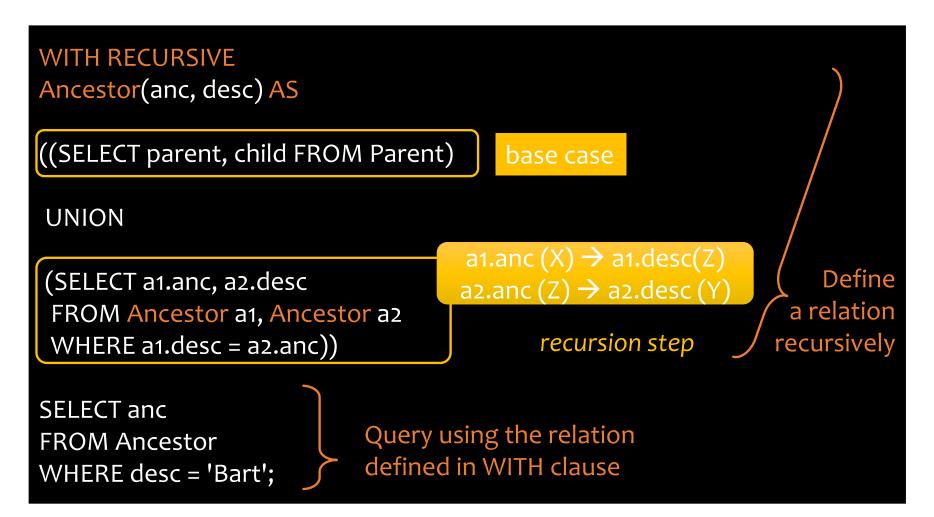
- Given any DML that violate the view's filter
 - If WITH CHECK OPTION: reject
 - If WITH CHECK OPTION is not specified: it is possible to "sneak" valid rows into the base table through the view -these rows simply won't appear in the view

Recursion Example



- Example: find Bart's ancestors
- "Ancestor" has a recursive definition
 - X is Y's ancestor if
 - X is Y's parent, or
 - X is Z's ancestor and Z is Y's ancestor

Example of Ancestor Query



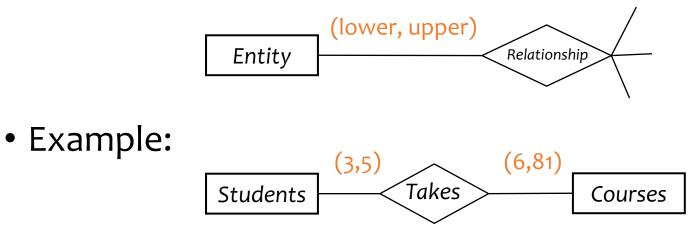
Database Design

E/R basics

- Entity: a "thing," like an object
- Entity set: a collection of things of the same type, like a relation of tuples or a class of objects
 - Represented as a rectangle
- Relationship: an association among entities
- Relationship set: a set of relationships of the same type (among same entity sets)
 - Represented as a diamond
- Attributes: properties of entities or relationships, like attributes of tuples or objects
 - Represented as ovals

General cardinality constraints

• General cardinality constraints determine lower and upper bounds on the number of relationships of a given relationship set in which a component entity may participate



• Total v.s. partial participation: (1,*) v.s. (0,*)

Weak entity sets

- If entity E's existence depends on entity F, then
 - F is a dominant entity
 - E is a subordinate entity

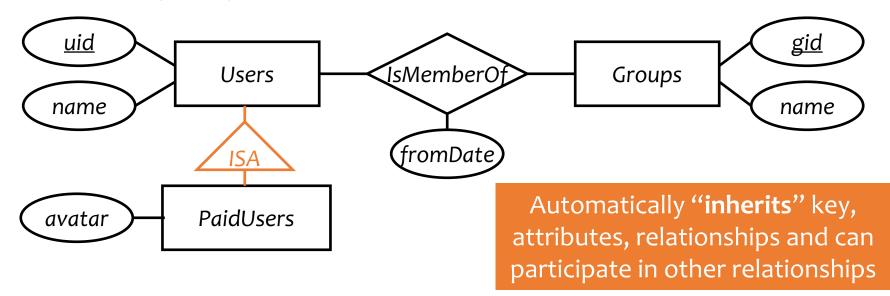
to a distinct entity set

 Example: Rooms inside Buildings are partly identified by Buildings' name 56

Weak entity set: containing subordinate entities
 Drawn as a double rectangle
 The relationship sets are called supporting relationship sets, drawn as double diamonds
 A weak entity set must have a many-to-one or one-to-one + total participation relationship

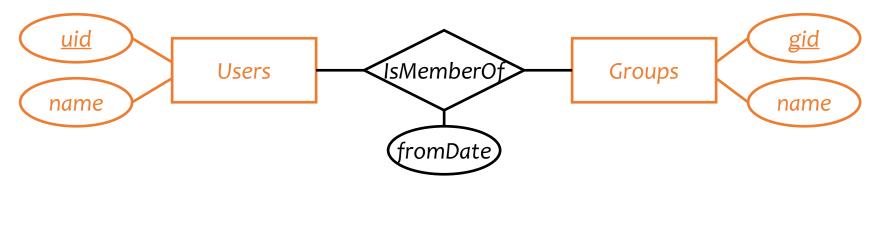
ISA relationships

- Similar to the idea of subclasses in object-oriented programming: subclass = special case, fewer entities, and possibly more properties
 - Represented as a triangle (direction is important)
- Example: paid users are users, but they also get avatars (yay!)



E/R Translation

- An entity set translates directly to a table
 - Attributes \rightarrow columns
 - Key attributes \rightarrow key columns

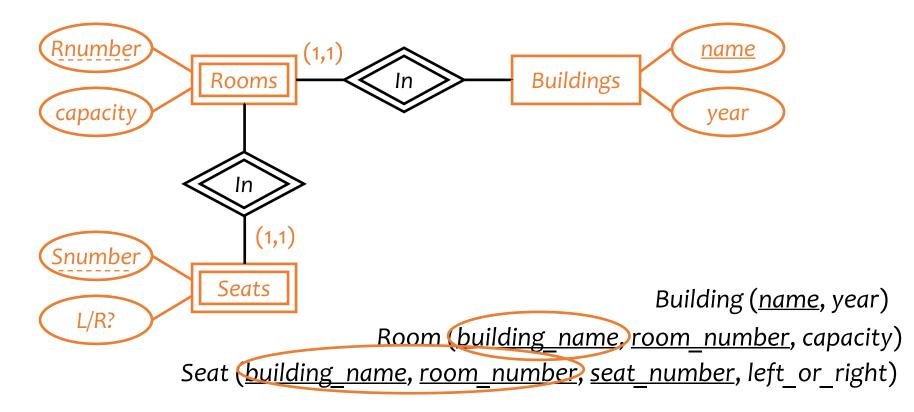


User (<u>uid</u>, name)

Group (<u>gid</u>, name)

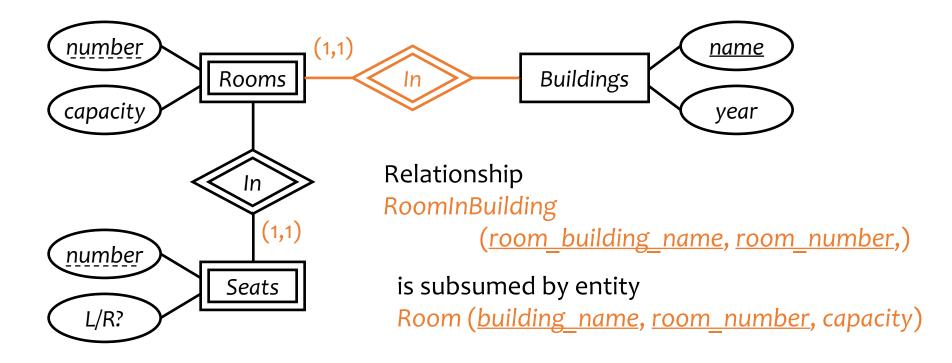
Translating weak entity sets

- Remember the "borrowed" key attributes
- Watch out for attribute name conflicts



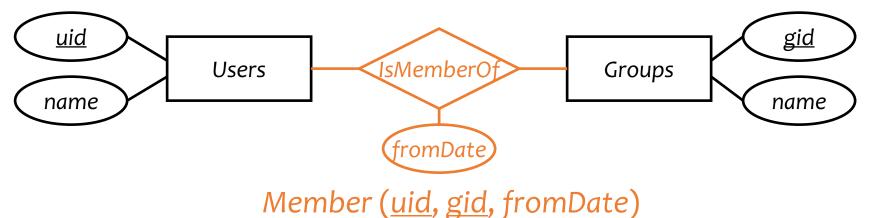
Translating double diamonds?

• No need to translate because the relationship is implicit in the weak entity set's translation



Translating relationship sets

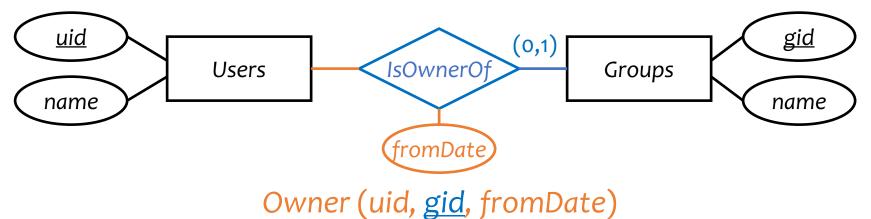
- A relationship set translates to a table
 - Keys of connected entity sets \rightarrow columns
 - Attributes of the relationship set (if any) \rightarrow columns
 - Multiplicity of the relationship set determines the key of the table



- If we can deduce the general cardinality constraint (0,1) for a component entity set E, then take the primary key attributes for E
- Otherwise, choose primary key attributes of each component entity

Translating relationship sets

- A relationship set translates to a table
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- If we can deduce the general cardinality constraint (0,1) for a component entity set E, then take the primary key attributes for E
- Otherwise, choose primary key attributes of each component entity

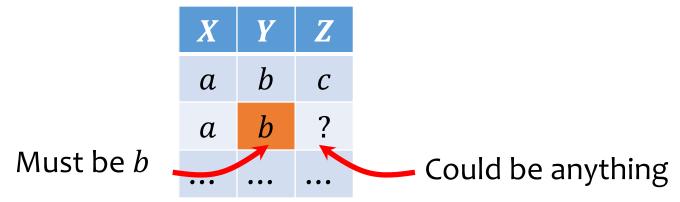
Translating subclasses & ISA

- Entity-in-all-superclasses
 - User (<u>uid</u>, name), PaidUser (<u>uid</u>, avatar)
 - Pro: All users are found in one table
 - Con: Attributes of paid users are scattered in different tables
- Entity-in-most-specific-class
 - User (<u>uid</u>, name), PaidUser (<u>uid</u>, name, avatar)
 - Pro: All attributes of paid users are found in one table
 - Con: Users are scattered in different tables
- All-entities-in-one-table
 - User (<u>uid</u>, [type], name, avatar)
 - Pro: Everything is in one table
 - Con: Lots of NULL's; complicated if class hierarchy is complex

Database Design theory

Functional dependencies

- A functional dependency (FD) is a constraint between two sets of attributes in a relation
- FD has the form $X \rightarrow Y$, where X and Y are sets of attributes in a relation R
 - whenever two tuples in *R* agree on all the attributes in *X*, they must also agree on all attributes in *Y*



• If X is a superkey of R, then $X \rightarrow R$ (all the attributes)

Armstrong's Axioms

- Reflexivity: if $Y \subseteq X$, then $X \rightarrow Y$
- Augmentation: if $X \rightarrow Y$, then $XZ \rightarrow YZ$
- Transitivity: if $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$

Implications of Armstrong's Axioms

- Decomposition: If $X \rightarrow YZ$, then $X \rightarrow Y$ and $X \rightarrow Z$
- Union: If $X \rightarrow Y$ and $X \rightarrow Z$ then $X \rightarrow YZ$
- Pseudo-transitivity: If $X \rightarrow Y$ and $YZ \rightarrow T$ then $XZ \rightarrow T$
- Using Armstrong's Axioms, you can prove or disprove a (derived) FD given a set of (base) FDs

Closure of FD sets: \mathcal{F}^+

- How do we know what additional FDs hold in a schema?
- A set of FDs \mathcal{F} logically implies a FD $X \to Y$ if $X \to Y$ holds in all instances of R that satisfy \mathcal{F}
- The closure of a FD set \mathcal{F} (denoted \mathcal{F}^+):
 - The set of all FDs that are logically implied by ${\mathcal F}$
 - Informally, \mathcal{F}^+ includes all of the FDs in \mathcal{F} , i.e., $\mathcal{F} \subseteq F^+$, plus any dependencies they imply.

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 \mathcal{F}^+

 ${\mathcal F}$

Attribute closure

- The closure of attributes Z in a relation R (denoted Z^+) with respect to a set of FDs, \mathcal{F} , is the set of all attributes $\{A_1, A_2, ...\}$ functionally determined by Z (that is, $Z \rightarrow A_1 A_2 ...$)
- Algorithm for computing the closure ComputeZ⁺(Z, F):
 - Start with closure = Z
 - If $X \rightarrow Y$ is in \mathcal{F} and X is already in the closure, then also add Y to the closure
 - Repeat until no new attributes can be added

Using attribute closure

Given a relation R and set of FD's \mathcal{F}

- Does another $FD X \rightarrow Y$ follow from \mathcal{F} ?
 - Compute X^+ with respect to \mathcal{F}
 - If $Y \subseteq X^+$, then $X \to Y$ follows from \mathcal{F}
- Is *K* a key of *R*?
 - Compute K^+ with respect to \mathcal{F}
 - If K⁺ contains all the attributes of R, K is a super key
 - Still need to verify that *K* is minimal (how?)
 - Hint: check the attribute closure of its proper subset.
 - i.e., Check that for no set X formed by removing attributes from K is K⁺the set of all attributes

Lossless decomposition

• We should be able to reconstruct the instance of the original table from the instances of the tables in the decomposition

A decomposition $\{R_1, R_2\}$ of R is lossless if and only if the common attributes of R_1 and R_2 form a superkey for either schema, i.e., $R_1 \cap R_2 \to R_1$ or $R_1 \cap R_2 \to R_2$

Dependency-preserving decomposition

• We should be able to (explicitly and implicitly) test all dependencies in each base table of the decomposition

Given a schema R and a set \mathcal{F} of FDs, decomposition of R is dependency preserving if there is an equivalent set \mathcal{F}' of FDs to \mathcal{F} , none FD in \mathcal{F}' is cross-table in the decomposition.

Boyce-Codd Normal Form (BCNF)

- A relation R is in BCNF under \mathcal{F} if each FD $X \to Y \in \mathcal{F}^+$ with $XY \subseteq R$ satisfies:
 - either $X \to Y$ is trivial, i.e., $Y \subseteq X$
 - or X is a super key of R, i.e., $X \rightarrow R$

 \mathcal{F} includes: A, B \rightarrow C C \rightarrow B

- Is $R = \{A, B, C\}$ under \mathcal{F} in BCNF? NO!
 - $C \rightarrow B$ is a violation since C is not a super key of R

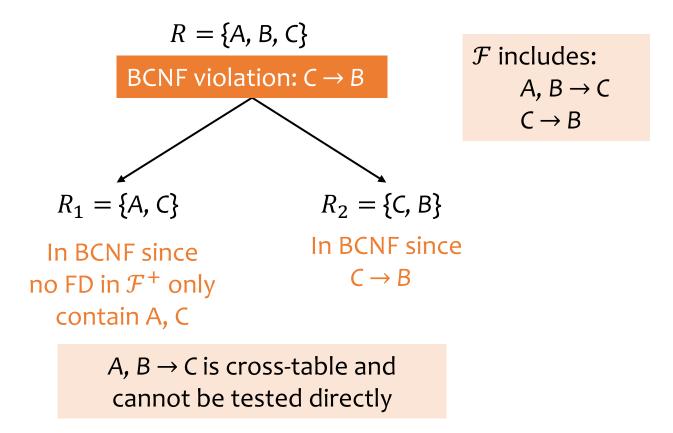
Compute BCNF decomposition

Repeat the following until all relations are in BCNF

- Step 1: Find a BCNF violation
 - A relation R
 - A non-trivial FD $X \to Y$ in \mathcal{F}^+ with $XY \subseteq R$, where X is not a super key of R
- Step 2: Decompose *R* into *R*₁ and *R*₂
 - R_1 has attributes $X \cup Y$;
 - R_2 has attributes $X \cup Z$, where Z contains all attributes of R that are in neither X nor Y
- BCNF is lossless!

Is BCNF dependency-preserving?

- NO!
- Consider a simple example R under \mathcal{F} :



Third normal form (3NF)

- A relation R is in 3NF under \mathcal{F} if each FD $X \rightarrow Y \in \mathcal{F}^+$ with $XY \subseteq R$ satisfies:
 - either $X \to Y$ is trivial, i.e., $Y \subseteq X$,
 - or X is a super key of R, i.e., $X \rightarrow R$ or,
 - or each attribute in Y X is in a key of R

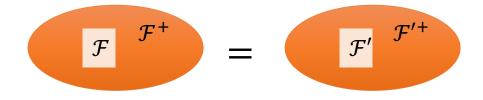
BCNF only allows the first two cases, so 3NF is looser than BCNF

- Is $R = \{A, B, C\}$ under \mathcal{F} in 3NF? YES!
 - A, $B \rightarrow C$ is satisfied since AB is a super key
 - $C \rightarrow B$ is satisfied since B is part of key $\{A, B\}$

 \mathcal{F} includes: $A, B \rightarrow C$ $C \rightarrow B$

Compute 3NF decomposition

- Step 1: Finding the minimal cover of the FD set ${\mathcal F}$



- Given a set of FDs \mathcal{F} , we say \mathcal{F}' is equivalent to \mathcal{F} if their closures are the same, i.e., $\mathcal{F}^+ = \mathcal{F}'^+$.
- The smallest equivalent set of FDs
- Step 2: Decompose based on the minimal cover

Minimal cover

A set of FDs $\mathcal F$ is minimal if

- every right-hand side of a FD in ${\mathcal F}$ is a single attribute
- there does not exist $X \to A$ with Z as a proper subset of X, such that $(\mathcal{F} \{X \to A\}) \cup \{Z \to A\}$ is equivalent to \mathcal{F}
- there does not exist $X \to A$ in \mathcal{F} such that $\mathcal{F} \{X \to A\}$ equivalent to \mathcal{F}

Compute minimal cover of $\mathcal F$

Repeat the following steps until $\mathcal F$ does not change

- Step 1: Replace $X \rightarrow YZ$ with $X \rightarrow Y$ and $X \rightarrow Z$
- Step 2: Remove *A* from the LHS of $X \rightarrow B$ if *B* is in the attribute closure of $X \{A\}$ until \mathcal{F}
- Step 3: Remove $X \to A$ if A is in the attribute closure of X under $\mathcal{F} \{X \to A\}$

Compute 3NF decomposition

Given a relation R with a set \mathcal{F} of FDs:

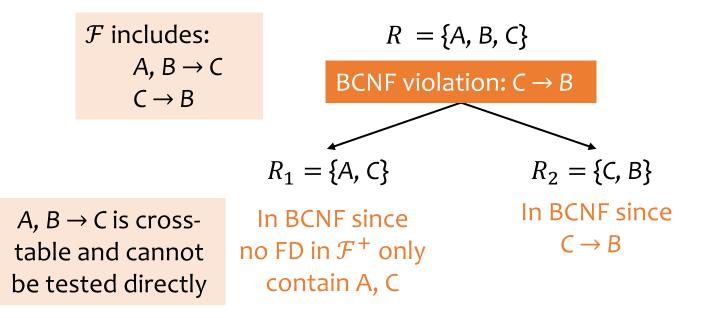
Step 1: Find a minimal cover \mathcal{F}^* for \mathcal{F}

Step 2: For every $X \to Y$ in \mathcal{F}^* , add a relation {X, Y} to the decomposition

Step 3: If no relation contains a key for R, add a relation containing an arbitrary key for R to the decomposition

BCNF v.s. 3NF

- Both BCNF and 3NF are lossless
- BCNF is not necessarily dependency-preserving but 3NF is dependency-preserving



• 3NF contains possible more redundancy than BCNF

