- Assignments should be completed individually.
- No late assignments will be accepted.
- Provide **concise** answers to the following questions. Use **point form** whenever possible.
- Submit your completed solutions to **Crowdmark**.

1. **Definition 1** *a **Hoare triple** is a triple $(\!|P|\!)\ C\ (\!|Q|\!)$ composed of*
   - *$P$, a **precondition** (an assertion),*
   - *$C$, some code, and*
   - *$Q$, a **postcondition** (another assertion).*

   **Definition 2** *A **specification** of a program $C$ is a Hoare triple with $C$ as the middle element of the triple.*

   **Definition 3** *A Hoare triple is **satisfied under partial correctness** if, whenever execution starts in a **state** satisfying precondition $P$, and terminates, it follows that the **state** after execution satisfies postcondition $Q$.*

   **Definition 4** *The **state** of a program at a given moment is the list of the values of each of its variables at that moment.*

   For each specification below, either
   - Give an informal argument for why the specification is satisfied under partial correctness, or
   - Give an example of a starting state which demonstrates that the specification is **not** satisfied under partial correctness, and briefly explain why your choice is correct.

[4] (a) $(\!|2 + y \geq 4|\!)$

```
x = 2;
```

$(\!|x + y \geq 4|\!)$

[4] (b) $(\!|x + y \geq 4|\!)$

```
x = 2;
```

$(\!|2 + y \geq 4|\!)$

2. It is mentioned in the Lecture Notes that **cost-benefit analysis** can be used to justify proving a software product is correct when human lives depend on correctness. One ethically problematic point about this practice is that it requires assigning a dollar value to a human life. In each of the following cases, assume that human lives depend on the correctness of the software product, and that your software professionals earn $2000 / week.

[2] (a) It is estimated that a new software product will require 12 person-weeks from a software professional for proving its correctness. The IT team manager authorizes spending the time to prove this software product is correct. What is the minimum dollar value of a human life in this cost-benefit analysis? Show your work.

[2] (b) It is estimated that another new software product will require 15 person-weeks from a software professional for proving its correctness. The IT team manager does not authorize spending the time to prove this software product is correct. What is the maximum dollar value of a human life in this cost-benefit analysis? Show your work.

3. In each part of this question, you will evaluate a software product, to assess the **cohesion** and **coupling** of its modules. The software product computes the **mean**, **median** and **mode** of a set of examination scores. Each software product is composed of two modules. In each part of the question,
   i. state whether the modules described have **high** or **low** cohesion, and briefly justify your answer, and
   ii. state whether the pair of modules described have **loose** or **tight** coupling, and briefly justify your answer.

[4] (a) This solution uses two classes, with the given properties/methods.

i. `list`

A. `property: mean`

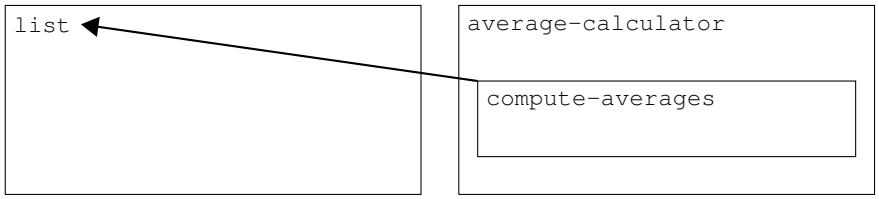
B. `property: median`

C. `property: mode`

ii. `average-calculator(my-list)`

A. `method: compute-averages`

```
/* return the triple
* (my-list.mean,my-list.median,my-list.mode)
*/
```



[4] (b) This solution uses two modules, with the given functions and descriptive comments.

i. average-calculator-1

A. total-entries(alist)

```
/* sum all entries in alist by calling
 * average-calculator-2.count-by-value(alist).
 */
```

B. sort-entries(alist)

```
/* return the entries of alist sorted non-descending.
 */
```

C. mode(alist)

```
/* return the mode of alist by calling
 * average-calculator-2.count-by-value(alist),
 * and returning a value with the highest count.
 */
```

ii. average-calculator-2

A. count-items(alist)

```
/* return the number of items in alist.
 */
```

B. count-by-value(alist)

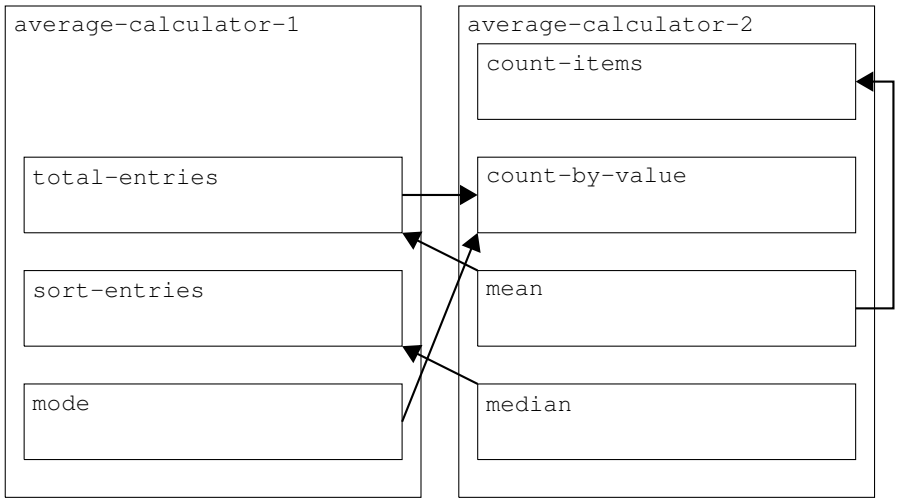
```
/* return a list of pairs (value, count)
 */
```

C. mean(alist)

```
/* compute the mean as the quotient
 * average-calculator-1.total-entries(alist)
 * over average-calculator-2.count-items(alist)
 */
```

D. median(alist)

```
/* compute the median as the middle element
 * or mean of the the middle two elements of
 * average-calculator-1.sort-entries(alist)
 */
```



[4] 4. Give an example of a pair of modules, `module-a` and `module-b`, such that
   i. each of `module-a` and `module-b` has **low** cohesion, and
   ii. the pair `module-a` and `module-b` has **loose** coupling.

   Briefly explain why your example is correct. Note, your description does not need to be highly detailed; describing the functionalities of `module-a` and `module-b` in broad strokes will suffice.