

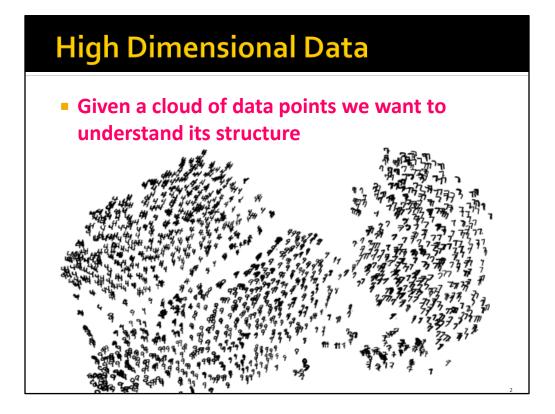
Data-Intensive Distributed Computing

CS 431/631 451/651 (Fall 2021)

Part 6: Data Mining (4/4)

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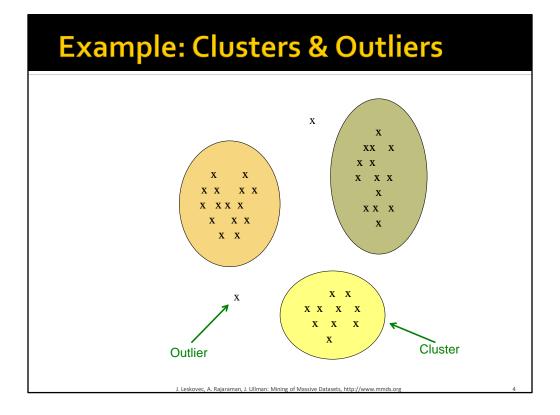
Thanks to Jure Leskovec, Anand Rajaraman, Jeff Ullman (Stanford University) These slides are available at https://www.student.cs.uwaterloo.ca/~cs451



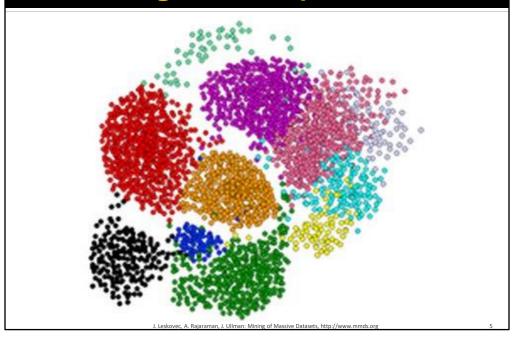
The Problem of Clustering

- Given a set of points, with a notion of distance between points, group the points into some number of *clusters*, so that
 - Members of a cluster are close/similar to each other
 - Members of different clusters are dissimilar
- Usually:
 - Points are in a high-dimensional space
 - Similarity is defined using a distance measure
 - Euclidean, Cosine, Jaccard, edit distance, ...

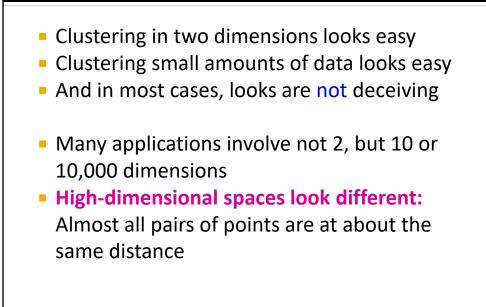
J. Leskovec, A. Rajaraman, J. Ullman: Mining of Massive Datasets, http://www.mmds.or



Clustering is a hard problem!



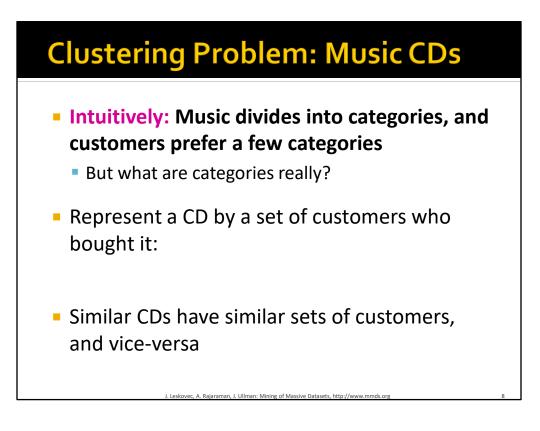
Why is it hard?

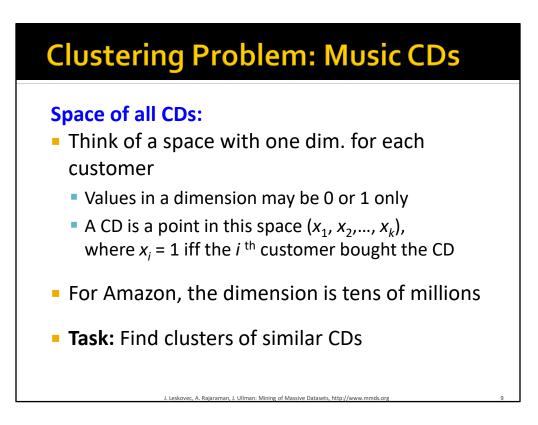


Clustering Problem: Galaxies

- A catalog of 2 billion "sky objects" represents objects by their radiation in 7 dimensions (frequency bands)
- Problem: Cluster into similar objects, e.g., galaxies, nearby stars, quasars, etc.
- Sloan Digital Sky Survey



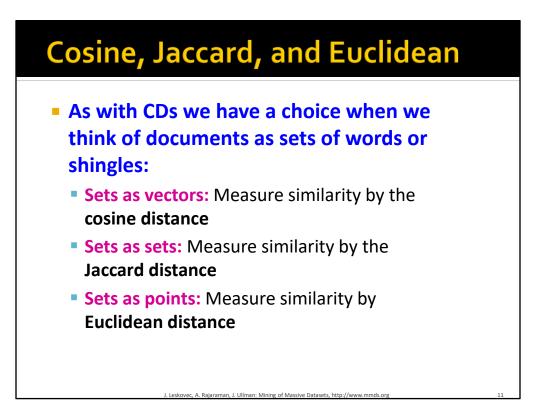


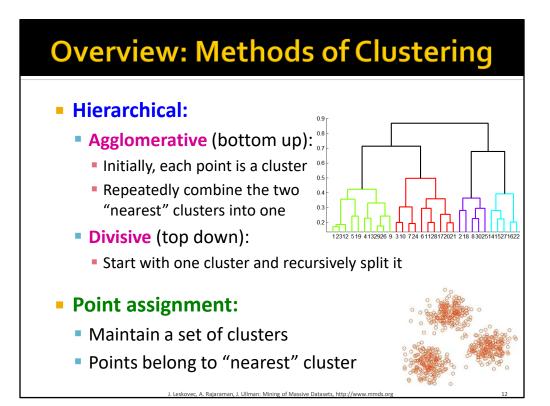


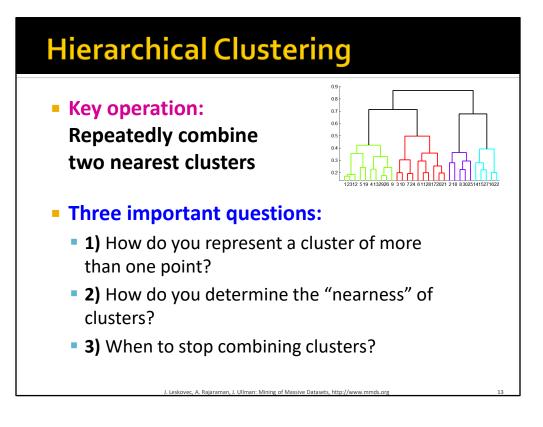
Clustering Problem: Documents

Finding topics:

- Represent a document by a vector (x₁, x₂,..., x_k), where x_i = 1 iff the *i* th word (in some order) appears in the document
 - It actually doesn't matter if k is infinite; i.e., we don't limit the set of words
- Documents with similar sets of words may be about the same topic





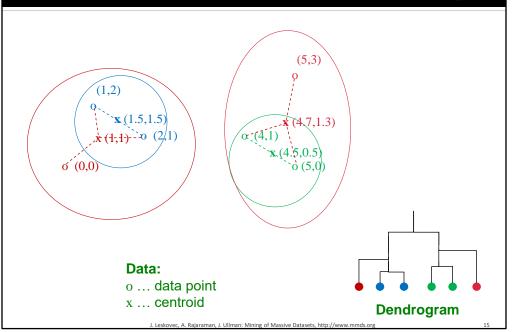


Hierarchical Clustering

- Key operation: Repeatedly combine two nearest clusters
 (1) How to represent a cluster of many points?
 Key problem: As you merge clusters, how do you represent the "location" of each cluster, to tell which pair of clusters is closest?
 Euclidean case: each cluster has a *centroid* = average of its (data)points
 (2) How to determine "nearness" of clusters?
 - Measure cluster distances by distances of centroids

. Leskovec, A. Rajaraman, J. Ullman: Mining of Massive Datasets, http://www.mmds.org

Example: Hierarchical clustering





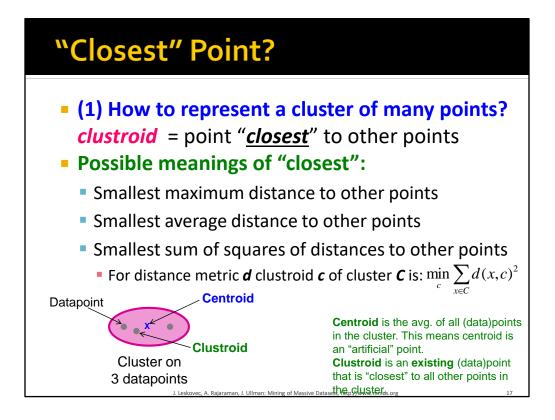
What about the Non-Euclidean case?

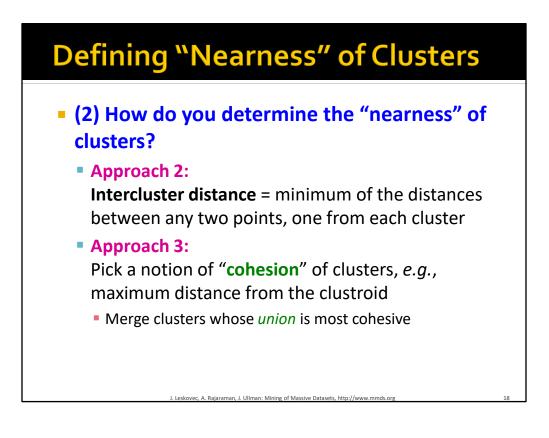
- The only "locations" we can talk about are the points themselves
 - i.e., there is no "average" of two points

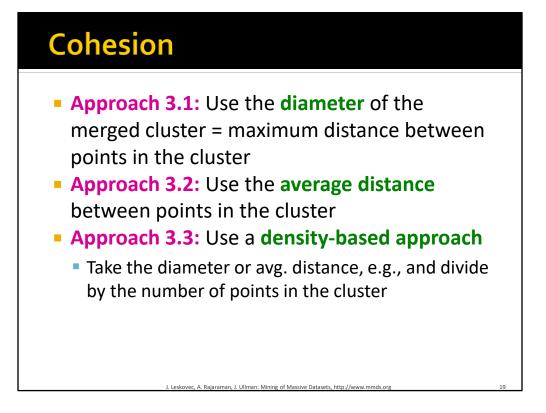
• Approach 1:

- (1) How to represent a cluster of many points?
 clustroid = (data)point "closest" to other points
- (2) How do you determine the "nearness" of clusters? Treat clustroid as if it were centroid, when computing inter-cluster distances

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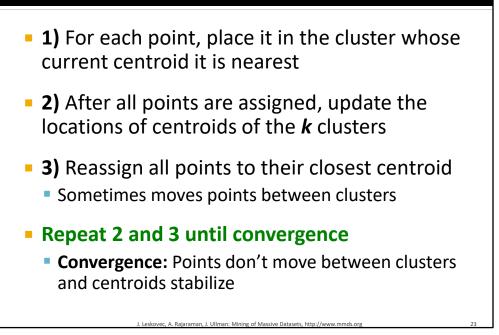
- Naïve implementation of hierarchical clustering:
 - At each step, compute pairwise distances between all pairs of clusters, then merge
 - O(N³)
- Careful implementation using priority queue can reduce time to O(N² log N)
 - Still too expensive for really big datasets that do not fit in memory

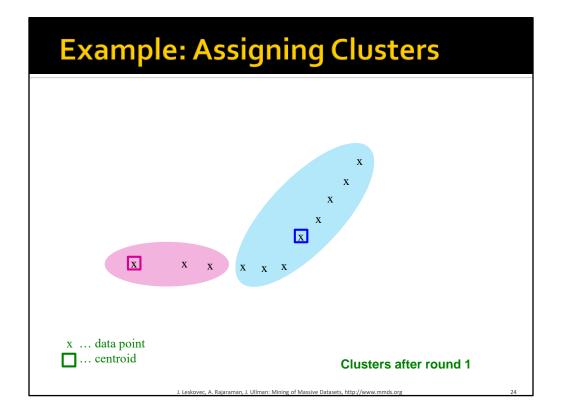
k-means clustering

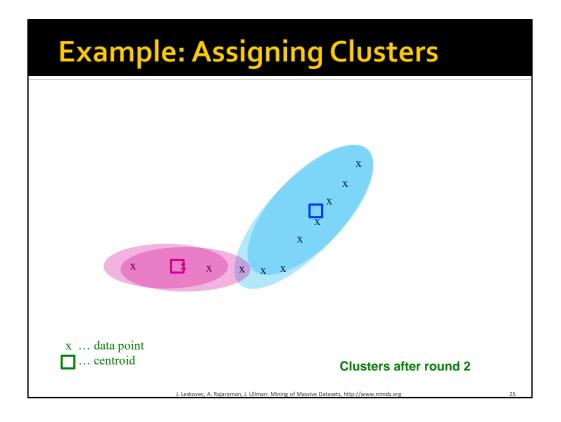
k–means Algorithm(s)

- Assumes Euclidean space/distance
- Start by picking *k*, the number of clusters
- Initialize clusters by picking one point per cluster
 - Example: Pick one point at random, then k-1 other points, each as far away as possible from the previous points

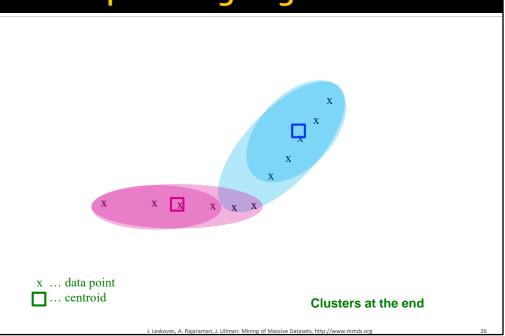
Populating Clusters







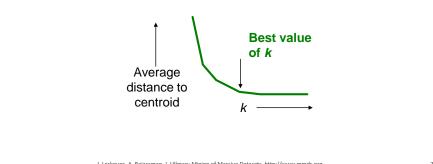
Example: Assigning Clusters

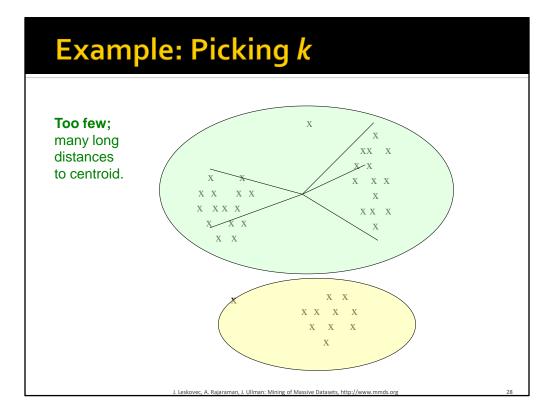


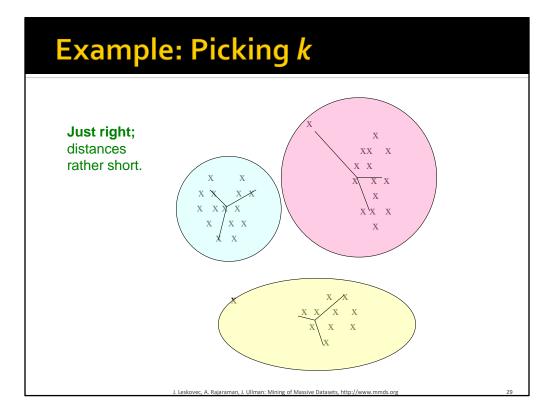
Getting the k right

How to select k?

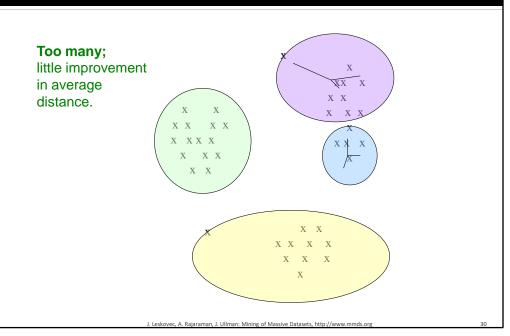
- Try different k, looking at the change in the average distance to centroid as k increases
- Average falls rapidly until right k, then changes little







Example: Picking *k*



class Mapper { def setup() = { clusters = loadClusters() } def map(id: Int, vector: Vector) = { emit(clusters.findNearest(vector), vector) } class Reducer { def reduce(clusterId: Int, values: Iterable[Vector]) = { for (vector <- values) { sum += vector cnt += 1 } </pre>

}

} }

emit(clusterId, sum/cnt)